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> restart;
f:=2*sin(y);
dfdy:=diff(f,y);
L:=int(sqrt(dfdy^2+1),y=Pi/6..5*Pi/6);
evalf(L);

```

$$\begin{aligned}
 f &:= 2 \sin(y) \\
 dfdy &:= 2 \cos(y) \\
 L &:= 2 \sqrt{5} \operatorname{EllipticE}\left(\frac{2}{5} \sqrt{5}\right) - 2 \sqrt{5} \operatorname{EllipticE}\left(\frac{1}{2}, \frac{2}{5} \sqrt{5}\right) \\
 &3.012453716
 \end{aligned}$$

```

> restart;
f:=x^(1/3)+4*x^(2/3);
dfdx:=diff(f,x);
L:=int(sqrt(dfdx^2+1),x=0..1);
evalf(L);

```

$$\begin{aligned}
 f &:= x^{(1/3)} + 4 x^{(2/3)} \\
 dfdx &:= \frac{1}{3 x^{(2/3)}} + \frac{8}{3 x^{(1/3)}} \\
 L &:= \int_0^1 \sqrt{\left(\frac{1}{3 x^{(2/3)}} + \frac{8}{3 x^{(1/3)}}\right)^2 + 1} dx \\
 &5.118694873
 \end{aligned}$$

```

> restart;
f:=tan(x);
dfdx:=diff(f,x);
A:=2*Pi*int(f*sqrt(dfdx^2+1),x=Pi/5..7*Pi/16);
evalf(A);

```

$$\begin{aligned}
 f &:= \tan(x) \\
 dfdx &:= 1 + \tan(x)^2 \\
 A &:= 2 \pi \int_{\frac{1}{5} \pi}^{\frac{7}{16} \pi} \tan(x) \sqrt{(1 + \tan(x)^2)^2 + 1} dx \\
 &78.67832836
 \end{aligned}$$

```

> restart;
f:=int(4*sin(t),t=0..y);

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dfdy:=diff(f,y);
A:=2*Pi*int(f*sqrt(dfdy^2+1),y=0..Pi/4);
evalf(A);
```

$$f := -4 \cos(y) + 4$$

$$dfdy := 4 \sin(y)$$

$$A := 2 \pi \left(4 \sqrt{17} \operatorname{EllipticE} \left(\frac{4}{17} \sqrt{17} \right) - 4 \sqrt{17} \operatorname{EllipticE} \left(\frac{1}{2} \sqrt{2}, \frac{4}{17} \sqrt{17} \right) \right. \\ \left. + \frac{\sqrt{\pi} + (-5 \ln(2) - 1) \sqrt{\pi} - 12 \sqrt{2} \sqrt{\pi} - 2 \sqrt{\pi} \ln \left(\frac{1}{2} + \frac{3}{8} \sqrt{2} \right)}{4 \sqrt{\pi}} \right)$$

4.767342002

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