

Sensitivity analysis:

$$S(t, c)$$

↖ exponential rate of growth of the fig. -

$$n(t) = 200 e^{ct}$$

Using the Pluto notebook interface...

```
julia> using Pluto
julia> Pluto.run()
[ Info: Loading...
[ Info:
Opening http://localhost:1234/?secret=EDiuOkQN in your default browser...
Have fun!
[ Info:
Press Ctrl+C in this terminal to stop Pluto
```

$$dPdt = -0.45 - 2.0 \exp(c*t) + 200c*(0.65 - 0.01t)*\exp(c*t) = u(t, c) = 0$$

$$dPdt = D(P(t), t)$$

$$S(t, c) = \frac{c}{t} \frac{dt}{dc} \Bigg| \approx \frac{c}{t} \frac{\Delta t}{\Delta c} = \frac{c_0}{t_0} \frac{(t_1 - t_0)}{(c_1 - c_0)} = 2.84$$

↖ Sensitivity of  $t$   
with respect to  
changes in  $c$   
at the best  
estimate ...

$$t = 19.46815944416122$$

$$c = 1/40$$

$$t_0 = 19.46815944416122$$

$$c_1 = (1.01) / 40$$

$$t_1 = 20.021136, \dots$$

with implicit differentiation

$$u(t, c) = 0$$

$$\frac{d}{dc} u(t, c) = \frac{d}{dc} 0$$

$$\frac{d}{dc} u(t, c) = \frac{\partial u}{\partial t} \frac{dt}{dc} + \frac{\partial u}{\partial c} = 0$$

$$\frac{dt}{dc} = - \frac{\partial u / \partial c}{\partial u / \partial t}$$

← compare with 2.84 from the book's estimate using  $\Delta t / \Delta c$  to approx  $dt/dc$ .

Stc = 2.8746311019686357

• Stc=substitute(c/t\*dtdc, [c=>1/40, t=>19.46815944415122])