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> restart;
> yp:=y(xn-h)+2*h*f(xn,y(xn));

$$yp := y(xn - h) + 2 h f(xn, y(xn)) \quad (1)$$

> ynp1:=y(xn)+h/2*(f(xn,y(xn))+f(xn+h,yp));

$$ynp1 := y(xn) + \frac{h(f(xn, y(xn)) + f(xn + h, y(xn - h) + 2 h f(xn, y(xn))))}{2} \quad (2)$$

> f:=(xi,eta)->A*eta;

$$f := (\xi, \eta) \mapsto A \eta \quad (3)$$

> method:=y(xn+h)=ynp1;

$$method := y(xn + h) = y(xn) + \frac{h(A y(xn) + A(y(xn - h) + 2 h A y(xn)))}{2} \quad (4)$$

> ceq:=eval(subs(y=(s->rho^s),method));

$$ceq := \rho^{xn + h} = \rho^{xn} + \frac{h(A \rho^{xn} + A(\rho^{xn - h} + 2 h A \rho^{xn}))}{2} \quad (5)$$

> ceq2:=subs({xn=0,h=1},ceq);

$$ceq2 := \rho = 1 + \frac{A}{2} + \frac{A \left( \frac{1}{\rho} + 2 A \right)}{2} \quad (6)$$

> S:=solve(ceq2,rho);

$$S := \frac{A^2}{2} + \frac{A}{4} + \frac{1}{2} + \frac{\sqrt{4 A^4 + 4 A^3 + 9 A^2 + 12 A + 4}}{4}, \frac{A^2}{2} + \frac{A}{4} + \frac{1}{2} - \frac{\sqrt{4 A^4 + 4 A^3 + 9 A^2 + 12 A + 4}}{4} \quad (7)$$

> # the linear stability region is all values of A such that |rho|<1
> Z1:=subs(A=a+I*b,abs(S[1]));

$$Z1 := \frac{1}{2} \left| (a + I b)^2 + \frac{a}{2} + \frac{I b}{2} + 1 + \frac{\sqrt{4 (a + I b)^4 + 4 (a + I b)^3 + 9 (a + I b)^2 + 12 a + 12 I b + 4}}{2} \right| \quad (8)$$

> Z2:=subs(A=a+I*b,abs(S[2]));

$$Z2 := \frac{1}{2} \left| (a + I b)^2 + \frac{a}{2} + \frac{I b}{2} + 1 - \frac{\sqrt{4 (a + I b)^4 + 4 (a + I b)^3 + 9 (a + I b)^2 + 12 a + 12 I b + 4}}{2} \right| \quad (9)$$

> with(plots):
> contourplot(max(Z1,Z2),a=-3..1,b=-2..2,contours=[1],grid=[100,100],filled=true);

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