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In[1]:= yp = y[xn - h] + 2 * h * f[xn, y[xn]]
Out[1]= 2 h f[xn, y[xn]] + y[-h + xn]

In[2]:= ynp1 = y[xn] + h / 2 * (f[xn, y[xn]] + f[xn + h, yp])
Out[2]=  $\frac{1}{2} h (f[xn, y[xn]] + f[h + xn, 2 h f[xn, y[xn]] + y[-h + xn]]) + y[xn]$ 

In[3]:= f = Function[{xi, eta}, A * eta]
Out[3]= Function[{xi, eta}, A eta]

In[4]:= method = y[xn + h] == ynp1
Out[4]= y[h + xn] == y[xn] +  $\frac{1}{2} h (A y[xn] + A (2 A h y[xn] + y[-h + xn]))$ 

In[5]:= ceq = method /. y → Function[s, rho^s]
Out[5]= rho^{h+xn} == rho^{xn} +  $\frac{1}{2} h \left( A rho^{xn} + A \left( 2 A h rho^{xn} + rho^{-h+xn} \right) \right)$ 

In[6]:= ceq2 = ceq /. {xn → 0, h → 1}
Out[6]= rho ==  $1 + \frac{1}{2} \left( A + A \left( 2 A + \frac{1}{rho} \right) \right)$ 

In[7]:= S = Solve[ceq2, rho]
Out[7]=  $\left\{ \begin{array}{l} rho \rightarrow \frac{1}{4} \left( 2 + A + 2 A^2 - \sqrt{4 + 12 A + 9 A^2 + 4 A^3 + 4 A^4} \right), \\ rho \rightarrow \frac{1}{4} \left( 2 + A + 2 A^2 + \sqrt{4 + 12 A + 9 A^2 + 4 A^3 + 4 A^4} \right) \end{array} \right\}$ 

In[8]:= ## the linear stability region is all values of A such that |rho| < 1
In[8]:= Z1t = Abs[rho] /. S[[1]]
Z1 = Z1t /. {A → a + I * b}
Out[8]=  $\frac{1}{4} \text{Abs} \left[ 2 + A + 2 A^2 - \sqrt{4 + 12 A + 9 A^2 + 4 A^3 + 4 A^4} \right]$ 
Out[9]=  $\frac{1}{4} \text{Abs} \left[ 2 + a - \sqrt{4 + 12 (a + i b) + 9 (a + i b)^2 + 4 (a + i b)^3 + 4 (a + i b)^4 + 2 (a + i b)^2 + i b} \right]$ 

In[10]:= Z2t = Abs[rho] /. S[[2]]
Z2 = Z2t /. {A → a + I * b}
Out[10]=  $\frac{1}{4} \text{Abs} \left[ 2 + A + 2 A^2 + \sqrt{4 + 12 A + 9 A^2 + 4 A^3 + 4 A^4} \right]$ 
Out[11]=  $\frac{1}{4} \text{Abs} \left[ 2 + a + \sqrt{4 + 12 (a + i b) + 9 (a + i b)^2 + 4 (a + i b)^3 + 4 (a + i b)^4 + 2 (a + i b)^2 + i b} \right]$ 

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In[12]:= ContourPlot[Max[Z1, Z2], {a, -3, 1}, {b, -2, 2}, Contours -> {1}, ContourShading -> {Red, Blue}]
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