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In[1]:= k1 = f[t, y[t]]
k2 = f[t + 2/5 * h, y[t] + 2/5 * h * k1]
k3 = f[t + 4/5 * h, y[t] - 1/5 * h * k1 + h * k2]
method = y[t + h] == y[t] + h * (1/6 * k1 + 5/12 * k2 + 5/12 * k3)

Out[1]= f[t, y[t]]

Out[2]= f[ $\frac{2h}{5} + t, \frac{2}{5}h f[t, y[t]] + y[t]$ ]

Out[3]= f[ $\frac{4h}{5} + t, -\frac{1}{5}h f[t, y[t]] + h f[\frac{2h}{5} + t, \frac{2}{5}h f[t, y[t]] + y[t]] + y[t]$ ]

Out[4]= y[h + t] == h  $\left( \frac{1}{6} f[t, y[t]] + \frac{5}{12} f[\frac{2h}{5} + t, \frac{2}{5}h f[t, y[t]] + y[t]] + \frac{5}{12} f[\frac{4h}{5} + t, -\frac{1}{5}h f[t, y[t]] + h f[\frac{2h}{5} + t, \frac{2}{5}h f[t, y[t]] + y[t]] + y[t]] \right) + y[t]$ 

In[7]:= f = Function[{t, y}, lambda * y]

Out[7]= Function[{t, y}, lambda y]

In[8]:= method

Out[8]= y[h + t] == y[t] + h  $\left( \frac{1}{6} \text{lambda } y[t] + \frac{5}{12} \text{lambda} \left( y[t] + \frac{2}{5}h \text{lambda } y[t] \right) + \frac{5}{12} \text{lambda} \left( y[t] - \frac{1}{5}h \text{lambda } y[t] + h \text{lambda} \left( y[t] + \frac{2}{5}h \text{lambda } y[t] \right) \right) \right)$ 

In[11]:= Simplify[method /. {h → 1, lambda → z}]

Out[11]= (6 + 6 z + 3 z2 + z3) y[t] == 6 y[1 + t]

In[12]:= r = (6 + 6 * z + 3 * z2 + z3) / 6

Out[12]=  $\frac{1}{6} (6 + 6 z + 3 z^2 + z^3)$ 

In[13]:= ra = Abs[r]

Out[13]=  $\frac{1}{6} \text{Abs}[6 + 6 z + 3 z^2 + z^3]$ 

In[14]:= ra2 = ra /. z → a + I * b

Out[14]=  $\frac{1}{6} \text{Abs}[6 + 6 (a + i b) + 3 (a + i b)^2 + (a + i b)^3]$ 

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In[16]:= ContourPlot [ra2, {a, -4, 2}, {b, -3, 3},  
Contours → {1}, ContourShading → {Red, Blue}]
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